taux d'occupation par Tl⁺ et par H_3O^+ ce qui donne le même pouvoir de diffusant que 0,6 Tl⁺). Cette dernière hypothèse est en accord avec la présence de H_3O^+ dans les sites monovalents observés dans les orthophosphates acides de fer, $Fe_3(H_3O)H_{14}(PO_4)_8.4H_2O$ (d'Yvoire, 1962), et d'aluminium, $Al_3(H_3O)H_{14}(PO_4)_8. 4H_2O$ (Brodalla & Kniep, 1980).

Les positions atomiques dans cette dernière structure (monoclinique C2/c) ont été entièrement déterminées, y compris celles des atomes d'hydrogène. L'isotypie de $Tl_3{Tl_{0.5}(H_3O)_{0.5}}H_{14}(PO_4)_8.4H_2O$ avec $Al_3(H_3O)H_{14}$ -(PO_4)_8.4H_2O est particulièrement frappante, si on décrit la structure du sel de thallium dans le repère monoclinique par la transformation:

$$\mathbf{a}_{mono} = -(\mathbf{a}_{tri} + \mathbf{b}_{tri}), \, \mathbf{b}_{mono} = \mathbf{a}_{tri}, \, \mathbf{c}_{mono} = \mathbf{c}_{tri}.$$

Cette étude montre qu'à côté des orthophosphates de thallium monovalents et trivalents, déjà connus, il existe aussi des orthophosphates de thallium à valence mixte.

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Structure of Dodecacalcium Potassium Fluoride Dioxide Tetrasilicate Bis(sulphate), KF.2[Ca₆(SO₄)(SiO₄)₂O]: a Fluorine-Containing Phase Encountered in Cement Clinker Production Process

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Abstract. $M_r = 1131.5$, trigonal, R3m, $a_H = 7.197$ (5), $c_H = 41.224$ (28) Å, V = 1894.3 Å³, Z = 3, $D_m = 2.92$, $D_x = 2.975$ Mg m⁻³, Mo Ka, $\lambda = 0.71069$ Å, $\mu = 3.06$ mm⁻¹, F(000) = 1692, room temperature, final R = 0.046 for 225 unique reflections; crystal selected from synthetic material. The crystal structure analysis confirms the chemical formula of the phase. The structure is related to that of tricalcium silicate (Ca₃SiO₅) and reveals the presence of rows containing oxide, sulphate, silicate and fluoride anions and six- (or twelve-) coordinate potassium, with seven-coordinate calcium on sites between the rows interconnecting them with Ca–O and Ca–F bonds.

Introduction. The title compound was described by Trivino Vazquez (1982) who isolated it from sedimentary coatings of Dopal kilns and designated it phase H. Since phase H was encountered in admixture with several other phases during its synthesis in the laboratory, there was some doubt as to its precise chemical composition and even as to its physical properties, *e.g.* density and X-ray powder diffraction pattern. Accordingly phase H has been prepared synthetically and an X-ray structure analysis carried out to characterize it more completely.

Experimental. Phase *H* was prepared by heating a stoichiometric mixture of $CaCO_3$, silica gel, K_2CO_3 and CaF_2 together with 6% (by weight) excess of KF and 6% excess of $CaSO_4$ at 1270 K for 1 h followed by crystallization of the melt at 1220 K for 48 h to yield crystals in the form of hexagonal plates suitable for further study. Electron microprobe analysis of the resulting crystals revealed the presence of Ca, K, S and Si in the ratio 1:0.09 (2):0.17 (1):0.32 (3) in agreement, within error, with the values 1:0.083:0.166: 0.333 calculated for the formula KF.2(Ca₆Si₂SO₁₃) as proposed for phase *H* by Trivino Vagquez (1982).

Measured density from Trivino Vazquez (1982); crystal flake $0.25 \times 0.15 \times 0.05$ mm. Intensities collected on Nicolet P3 diffractometer, graphite monochromator, Mo Ka; unit cell from 14 reflections in range $19 \le 2\theta \le 23^{\circ}$. No absorption correction. Data collected in range $0 \le 2\theta \le 40^{\circ}$, $\omega/2\theta$ scan method; h,k,l in ranges $0 \le h,k \le 5$ and $-40 \le l \le 40$; standard reflections 0,0,15 and 207 showed no significant variation. 364 reflections measured (for Laue group $\overline{3}$); 246 unique (for Laue group $\overline{3}m$); 21 unobserved $[I < 2\sigma(I)]$ not used in calculations. Partial solution of structure from MULTAN80 (Main *et al.*, 1980), completed by Fourier methods; block-diagonal least

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squares minimized $\sum w(|F_{o}| - |F_{c}|)^{2}$, $w = [1 + \{(F_{o} - |F_{c}|)^{2}, w]$ (110)/60²]⁻¹; in final stages of refinement O and F treated isotropically, all other atoms anisotropic. Final shifts in positional parameters essentially zero and av. $\Delta = 0.1\sigma$ with no feature in difference map exceeding $0.7 e^{-1}$. Atomic scattering factors for neutral O, F, S and Si and K⁺ and Ca²⁺ from International Tables for X-ray Crystallography (1974); programs used were MULTAN80 (Main et al., 1980), the NRC Crystallographic Programs (Ahmed, Hall, Pippy & Huber, 1966), STRUPLO82 (Fischer, 1982) for the preparation of Figs. 1 and 2 and POWD (Howie & Taylor, 1978) to calculate the theoretical powder pattern.

Intensity data collection was initially confined to the unique reflections appropriate to the Laue group $\overline{3}$. The data showed excellent agreement between the intensities in the reflection pairs hkl and khl consistent with Laue group $\overline{3}m$. The data were averaged on this basis. The space group of phase H must then be one of R32, R3m or $R\overline{3}m$. $R\overline{3}m$ was adopted as suggested by the distribution of E values given by MULTAN80. This choice was confirmed by the successful outcome of the structure analysis.

The final atomic parameters are given in Table 1 and selected bond lengths and angles in Table 2.*

Discussion. The structure determination of phase H gives an indication of its chemical composition independently of chemical analysis or microprobe results. The distinction between SO_4 and SiO_4 is readily made on the basis of bond lengths alone (Table 2). There is also evidence confirming the identity of the atom at $00\frac{1}{2}$ as F rather than O. Least-squares refinement with all non-(O or F) atoms correctly identified and all atoms vibrating isotropically but with O at $00\frac{1}{2}$ gave a negative B_{iso} for the atom at this site and R = 0.054. Refinement with F at $00\frac{1}{2}$ gave satisfactory B's for all atoms and R = 0.053. The cell contents are then 3[KFCa₁₂- $(SO_4)_2(SiO_4)_4O_2$, agreeing exactly with the formula given by Trivino Vazquez (1982).

The completed structure of phase H (Figs. 1 and 2) reveals SO₄, SiO₄ and O²⁻ anions in the 6(c) sites of $R\overline{3}m$ with site symmetry 3m and K and F in the 3(a)and 3(b) sites with site symmetry $\overline{3}m$. These components of the structure lie on the rows 00z, $\frac{12}{33}z$ and $\frac{21}{33}z$ (threefold axes parallel to c) and fall in the order

 \cdots K/Si(1)O₄/Si(2)O₄/SO₄/O/F \cdots

with centres of symmetry at K and F sites. Ca occupies two sets of 18(h) sites between the rows and inter-

Table 1.	Fractional	coordinate	$es (\times 10^4)$	and is	sotropic
therma	l parameter.	s (Å ² ×10).	for KF.2	(Ca ₆ Si ₂	SO ₁)

Values	in	parentheses	are	e.s.d.'s	corresponding	to	the	least
			sigr	nificant d	igit.			

	Wyckoff	r*	7	R
C-(1)	10(4)	1502 (2)	2050 0 (0)	D 150
Ca(1)	18(<i>n</i>)	1593 (2)	39/8-8 (2)	8.91
Ca(2)	18(<i>h</i>)	1533 (2)	5324.4 (3)	8.0†
O(1)	18(h)	5564 (6)	-3548.2 (8)	14.7 (7)
O(11)	18(<i>h</i>)	1235 (6)	1946.0 (8)	13.3 (6)
O(21)	18(h)	1261 (5)	728.1 (8)	11.3 (6)
O(2)	6(c)	0	-3604 (1)	10(1)
O(12)	6(c)	0	-2464 (1)	12(1)
O(22)	6(c)	0	1233 (1)	8 (1)
O(3)	6(<i>c</i>)	0	4303 (1)	5 (1)
S(1)	6(c)	0	-3243.8 (5)	7.3+
Si(1)	6(<i>c</i>)	0	2064.4 (6)	7.1+
Si(2)	6(c)	0	832.3 (6)	7.8†
K(1)	3(a)	0	0	21.3†
F(1)	3(<i>b</i>)	0	5000	14 (1)

* All atomic coordinates are of the form $x \bar{x} z$. Only x and z are quoted.

† Equivalent B_{iso} calculated as $\frac{4}{3}(B_{11}a^2 + B_{22}b^2 + B_{33}c^2 + B_{12}ab/2).$

Table 2. Selected bond lengths (Å) and angles (°) for $KF.2(Ca_6Si_2SO_{13})$

Values in parentheses are e.s.d.'s applicable to the least significant digit of each entry.

K(1)-O(1 ^{v1}) O(21)	2.919 (4) ×6 3.388 (3) ×6		
S(1)-O(1) O(2) O(1)-O(1) O(2)	1·468 (4) ×3 1·484 (6) 2·381 (5) 2·427 (6)	O(1)-S(1)-O(1) O(1)-S(1)-O(2)	108·3 (2) ×3 110·6 (2) ×3
Si(1)-O(11) O(12) O(11)-O(11) O(12)	1.615 (4) ×3 1.649 (6) 2.667 (5) 2.634 (6)	O(11)–Si(1)–O(11) O(11)–Si(1)–O(12)) 111.3 (2) ×3) 107.6 (2) ×3
Si(2)–O(21) O(22) O(21)–O(21) O(22)	1.630 (4) ×3 1.653 (6) 2.723 (5) 2.610 (6)	O(21)–Si(2)–O(21) O(21)–Si(2)–O(22)) 113·3 (2) ×3) 105·3 (2) ×3
Ca(1)-O(3) O(2 ¹) O(1 ¹¹) O(21 ¹¹¹) O(12 ¹¹)	2-394 (3) 2-517 (4) 2-601 (4) ×2 2-367 (4) ×2 2-357 (2)	Ca(2)-F O(3 ^{II}) O(11) O(21 ^v) O(22 ^v) O(11 ^{III})	2·332 (1) 2·452 (3) 2·587 (4) 2·620 (4) 2·289 (2) 2·351 (4) ×2

Symmetry code: (i) -x, x, -z; (ii) 2x - 1, x - 1, -z and 1 - x, $1 - 2x, -z; (iii) \frac{2}{3} - 2x, \frac{1}{3} - x, \frac{1}{3} + z \text{ and } x - \frac{1}{3}, 2x - \frac{2}{3}, \frac{1}{3} + z; (iv) \frac{1}{3} + x, -x - \frac{1}{3}, \frac{2}{3} + z; (v) \frac{1}{3} - x, x - \frac{1}{3}, \frac{2}{3} - z; (vi) \text{ as (iii) with } x - \frac{1}{3}, \frac{1}{3} - x, \frac{1}{3} + z \text{ and three more from } \overline{1} \text{ at K}; \text{ otherwise O(1), O(11) and}$ O(21) are replicated as x, \overline{x} , z; x, 2x, z and $2\overline{x}$, \overline{x} , z.

connects them with Ca-O and Ca-F bonds. K-O bonds also contribute to the interconnection between the rows and possibly to connections within the rows. Viewed in this way there are definite similarities between the structure of phase H and that determined for Ca₃SiO₅ by Jeffery (1952). In the rhombohedral structure of Ca₃SiO₅ the rows parallel

^{*} Lists of structure factors, anisotropic thermal parameters, observed and calculated X-ray powder diffraction data and a full list of interatomic lengths and angles have been deposited with the British Library Lending Division as Supplementary Publication No. SUP 42032 (30 pp.). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 5 Abbey Square, Chester CH1 2HU, England.

to **c** contain alternating sets of three O and three SiO_4 groups.

$$\cdots O - O - O - SiO_4 - SiO_4 - SiO_4 \cdots$$

The rows of anions in Ca₃SiO₅ are again interconnected by Ca–O bonds to Ca in sites between them. Jeffery (1952) pointed out that within any one set of three SiO₄ groups one SiO₄ is rotated through 60° about the *c* axis relative to the other two. Exactly the same feature is observed in the structure of phase *H* where within any single group of $1 \times SO_4$ and $2 \times SiO_4$ the SO₄ is rotated 60° relative to the pair of eclipsed SiO₄ ions (viewed along c). The main differences between the structures of Ca₃SiO₅ and phase *H* are: (i) the presence of K in the rows of phase *H*; (ii) F in phase *H* replaces O(5)* in Ca₃SiO₅; (iii) SO₄ in phase *H* replaces Si(1)O^{*}₄ in Ca₃SiO₅ and (iv) the rows in phase *H* possess centres of symmetry.

The SO_4 and SiO_4 ions of phase *H* have bond distances and angles in the usual range (Table 2). Both

* Atom numbering according to Jeffery (1952).



Fig. 1. Projection of one half of the unit cell of KF.2(Ca₆Si₂SO₁₃) $(z = 0 - \frac{1}{2})$ on (001). SiO₄ and SO₄ (marked S) are shown as tetrahedra. F and Ca are shown as large and small circles. O is not visible in this representation.



Fig. 2. Section of the structure of $KF.2(Ca_6Si_2SO_{13})$ close to (110). SiO₄ and SO₄ (marked S) are shown as tetrahedra. F (marked) and O and K (marked) and Ca lying on the plane of the section are shown as large and small circles respectively.

Ca atoms are seven-coordinate (Table 2) and the coordination is in each case that of a pentagonal bipyramid and includes an edge shared with a tetrahedral ion. Ca(1) is coordinated only to O with Ca-O in the range 2.357-2.601 Å; O(12^{iv}) and O(2ⁱ) are the apical atoms. The other atoms lie close to a plane at right angles to the crystallographic mirror plane passing through Ca(1); the out-of-plane distances for the O atoms defining the plane (mean value) and for Ca(1) are 0.05(6) and 0.28(6) Å respectively. The two O(1ⁱⁱ) define an edge of an SO₄ tetrahedron, which is thus bidentate with respect to completing the Ca coordination, Ca(2) is coordinated to O (Ca-O 2.289-2.620 Å) and to F (Ca-F 2.332 Å). The apical atoms are O(11ⁱⁱⁱ) (twice) and the pentagonal base of the pyramid lies in the crystallographic mirror plane passing through Ca(2). $O(21^{v})$ and $O(22^{v})$ define the edge of an SiO₄ tetrahedron. K has six nearestneighbour O(1) at 2.919 Å (Table 2) distributed over the apices of a rather flattened trigonal anti-prism. The next-nearest atoms are six O(21) at 3.388 Å belonging to SiO₄ groups above and below K and in the same row parallel to c. This rather distorted coordination may account for the relatively high thermal vibration parameter for K.

The X-ray powder diffraction data observed for phase *H* by Trivino Vazquez (1982) are in good agreement with values calculated from the final parameters of the structure analysis.* No spacing is found on the calculated pattern to match those observed at 1.885, 1.797, 1.592, 1.505, 2.051 and 1.589 Å. However, each of the first four 'missing' spacings corresponds in position and intensity to the α_2 component of an adjacent reflection and the program *POWD* (Howie & Taylor, 1978) is designed to delete such lines from the calculated pattern. Only the last two weak spacings cannot be accounted for and presumably arise from impurity phases.

* See deposition footnote.

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